

Fourth Semester B.E. Degree Examination, June / July 08
Control Systems

Time: 3 hrs.

Max. Marks:100

Note : Answer FIVE full questions, choosing atleast two questions from each part.

PART - A

- 1 a. Define control system. Compare open loop and closed loop control system with two examples for each type. (08 Marks)
- b. Obtain differential equations describing the mechanical system shown in Fig. Q 1(b). Then draw electric circuits based on F-V and F-I analogy. (12 Marks)

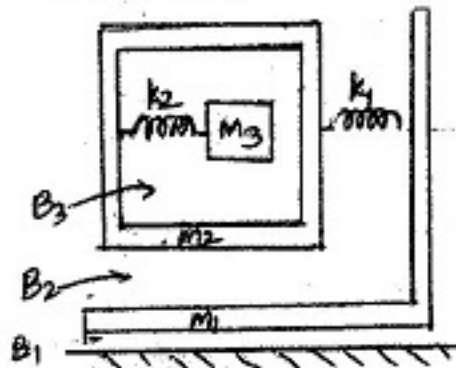


Fig. Q 1(b)

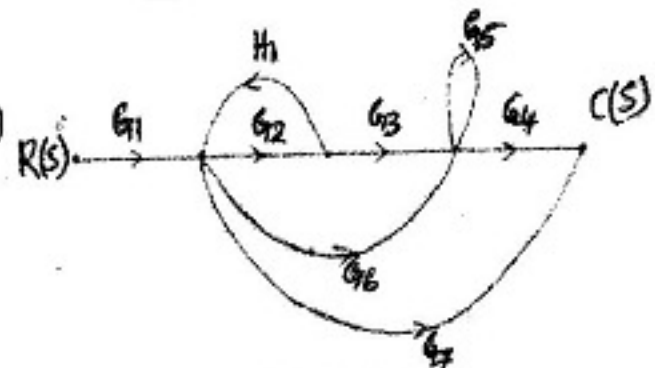


Fig. Q 2(a)

- 2 a. Find $C(S) / R(S)$ for the signal flow graph shown in Fig. Q 2(a) using Mason's gain formula. (10 Marks)
- b. Determine the transfer function of a system whose block diagram is given in Fig. Q 2(b) below using the block diagram reduction technique. (10 Marks)

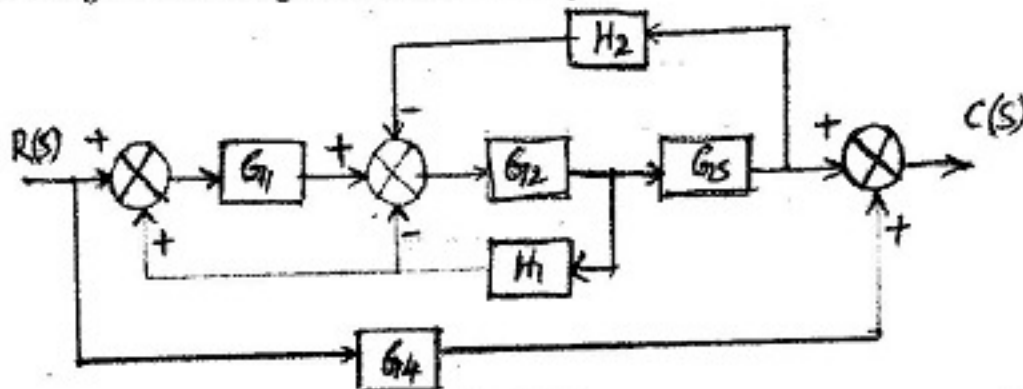


Fig. Q 2(b)

- 3 a. The open loop transfer function of an unity feed back control system is given by $G(s) = K/S(1 + TS)$ (08 Marks)
- i) By what factor should the amplifier gain K be multiplied in order that the damping ratio is increased from 0.2 to 0.8?
- ii) By what factor should K be multiplied so that the system overshoot for unit step excitation is reduced from 60% to 20%.
- b. Find the position, velocity and acceleration error constant for a control system having open loop transfer function $GH(s) = \frac{4}{s(s+1)(s+2)}$. Also determine its steady state error for a unit step, ramp and parabolic inputs. What is the steady state error due to the transform input of $R(S) = \frac{2}{s} - \frac{1}{s^2}$. (08 Marks)
- c. Derive an expression for generalized error coefficients. (04 Marks)

- 4 a. A system oscillates with a frequency ω rad/sec if it has poles at $S = \pm j\omega$ and no poles in right half of the S -planes. Determine the value of 'K' and 'a' so that the system shown in Fig. Q 4(a) below oscillates at a frequency of 2 rad/sec.

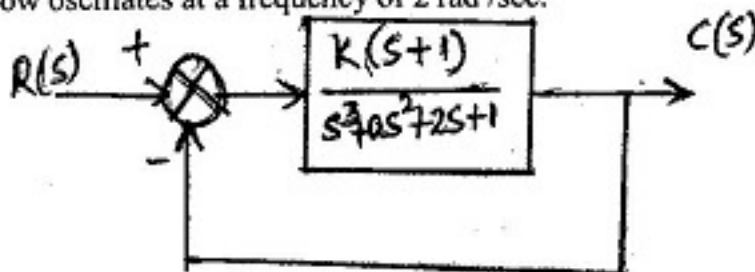


Fig. Q 4(a)

(10 Marks)

- b. Determine the ranges of K such that the characteristic equation $s^3 = (2k+3)s^2(6k+7)s + (7k+8.5) = 0$ has roots more negative than $s = -1$.

(10 Marks)

PART - B

- 5 a. Sketch the root locus and hence determine :
- The damping ratio and the corresponding value of K for maximum damped oscillatory response.
 - The closed loop transfer function corresponding to (i) for a unity feed back system having $G(s) = \frac{k(s+3)}{s(s+2)}$.

(10 Marks)

- b. Discuss with a suitable example the importance of root locus diagram.

(10 Marks)

- 6 a. State and explain Nyquist stability criterion.

(08 Marks)

- b. Draw the Nyquist plot for the given open loop transfer function $GH(s) = \frac{10(s+1)}{s^2(1+0.25s)}$.

Determine the stability of the system using Nyquist stability criterion.

(12 Marks)

- 7 a. The open loop transfer function of a unity feed back control system is given by

$$G(s) = \frac{k(s+1)}{s(1+0.1s)^2(1+0.02s)}$$

- Draw the Bode plot and hence find phase margin and gain margin for $K = 1$.
 - Determine the value of 'K' for a gain margin of 20 dB and the value of 'K' for a phase margin of 30° .
- b. Determine the transfer function of the given system whose Bode magnitude plot is as shown in Fig. Q 7(b).

(14 Marks)

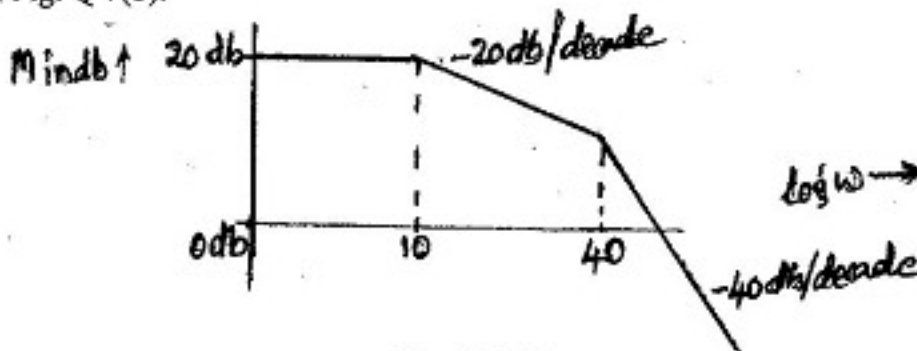


Fig. Q 7(a)

(06 Marks)

- 8 a. Write state space equation for the following equation :

$$L_a \frac{di_a}{dt} + R_a i_a + k_b \theta = V_a(t) \quad \text{and} \quad J \frac{d^2\theta}{dt^2} + f \frac{d\theta}{dt} = T_a(t) \quad \text{where} \quad T_a(t) = K_t i_a.$$

(08 Marks)

- b. Write short notes on :

(12 Marks)

- State transition matrix
- State space analysis
- Phase margin and gain margin.
